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The periodictable package provides an extensible periodic table of the elements pre-populated with data important to neutron and X-ray scattering experiments. Periodic table is written entirely in Python and does not require any external libraries.
This section gives an overview and introduction to Periodic Table. Read this to have an idea about what Periodic Table can do for you (and how) and if you want to know in detail about Periodic Table, refer to the Periodic Table Modules Reference.

1.1 Periodic Table of Elements

The periodictable package provides an extensible periodic table with various properties of the elements like name, symbol, mass, density etc and also provides data important to neutron and X-ray scattering experiments. With the elements package you can compute the scattering potential of a compound at a given wavelength.

There is a wealth of possible information that could be stored in such a table, and collecting it all is far beyond the scope of this project. Instead, we provide an extensible table in which third party packages can provide properties in addition to the base properties we define here.
Neutron SLD as a function of element.

### 1.1.1 Features

**Standard properties** Name, symbol, **mass** and **density** of elements are built in.

**Chemical Formula** Parses chemical formula and computes properties such as molar mass.

**Isotopes** Mass and relative abundance of isotopes are included for known isotopes. Formulas can include isotope composition.

**Ions** Magnetic form factors and ionic radii for various ions.

**Neutron and X-ray Scattering Factors** Provides neutron and wavelength dependent X-ray scattering factors for elements, isotopes, and formulas.

**Extensible** New properties can be added to the Periodic Table from outside the package. Specialized tables can be created with alternatives to the standard values.

**Data Sources** References are available for all information in the table.
1.2 Installing

This tutorial will walk you through the process of installing Periodic Table. To follow, you only need two basic things:

- A working Python installation, version 2.4 or higher.
- Easy_install module, if you don’t have easy_install installed on your system, download here.

The periodic table will be provided as an egg on PyPI, and can be obtained simply with:

```python
[coming soon] easy_install periodictable
```

The source is available via svn:

```
svn co svn://danse.us/common/elements/trunk periodictable
cd periodictable
python setup.py develop
```

Track updates to the package using:

```
svn update
```

By using the `develop` keyword on setup.py, you can modify and update the package in place without needing to reinstall each time.

If you find you need to modify the periodic table package, please generate a patch and send it to the DANSE Project mailing list at danse-dev@cacr.caltech.edu:

```
svn diff > periodictable.patch
```

Windows user can use TortoiseSVN package which provides similar operations.

1.3 Basic usage

This section provides various examples on how to get started with Periodic table. These examples should work on all periodic table supported platforms.

Access particular elements by name:

```python
>>> from periodictable import hydrogen
>>> print "H mass", hydrogen.mass, hydrogen.mass_units
H mass 1.00794 u
```

Access particular elements as symbols:

```python
>>> from periodictable import H,B,Cu,Ni
>>> print "B absorption", B.neutron.absorption
B absorption 767.0
>>> print "Ni f1/f2 for Cu K-alpha X-rays", Ni.xray.scattering_factors(Cu.K_alpha)
Ni f1/f2 for Cu K-alpha X-rays (27.13235204490778, 8.403244506816351)
```

Access isotopes using mass number subscripts:

```python
>>> print "58-Ni vs 62-Ni scattering", Ni[58].neutron.coherent, Ni[62].neutron.coherent
58-Ni vs 62-Ni scattering 26.1 9.5
```
Access elements indirectly:

```python
>>> import periodictable
>>> print "Cd density", periodictable.Cd.density, periodictable.Cd.density_units
Cd density 8.65 g/cm**3
```

Import all elements:

```python
>>> from periodictable import *
>>> print periodictable.H
H
>>> print periodictable.H.mass
1.00794
```

Deuterium and tritium are special isotopes named D and T some neutron information is available as ‘n’:

```python
>>> print "D mass", D.mass
D mass 2.014101778
>>> print "neutron mass", n.mass
neutron mass 1.00866491597
```

Process all the elements:

```python
>>> # importing periodic table as "import periodictable"
>>> for el in periodictable.elements:
...     print el.symbol, el.name
n neutron
H hydrogen
He helium
...
Uuh ununhexium
```

Another example for processing all elements:

```python
>>> # importing periodic table as "from periodictable import *"
>>> for el in elements:
...     print el.symbol, el.number
n 0
H 1
He 2
...
```

Process all the isotopes for an element:

```python
>>> for iso in periodictable.H:
...     print iso, iso.mass
1-H 1.0078250321
D 2.014101778
T 3.0160492675
4-H 4.02783
5-H 5.03954
6-H 6.04494
```

Retrieve ion specific properties such as magnetic form factor:
You can create a unique handle to an individual ion. In addition to storing the ion charge, this can be used to reference the underlying properties of the element or isotope:

```python
define Ni58_2 = periodictable.Ni[58].ion(2)
define Ni_2 = periodictable.Ni.ion(2)
print "charge for Ni2+", Ni_2.charge
charge for Ni2+ 2
print "mass for Ni[58] and for natural abundance", Ni58_2.mass, Ni_2.mass
mass for Ni[58] and for natural abundance 57.9353479 58.6934
```

The ion specific properties can be accessed from the ion using ion.charge for the ion index:

```python
import pylab
import periodictable
Fe_2 = periodictable.Fe.ion(2)
Q = pylab.linspace(0,16,200)
M = Fe_2.magnetic_ff[Fe_2.charge].j0_Q(Q)
pylab.xlabel(r'Magnetic Form Factor for Fe$
pylab.ylabel(r'$\AA^{-1}$')
pylab.title('Ion specific property for Fe')
pylab.plot(Q,M)
```
Missing properties generally evaluate to None:

```python
>>> print "Radon density",periodictable.Rn.density
Radon density None
```

Specific defined properties related to elements can be accessed in a table format as shown in following example:

```python
>>> elements.list('symbol','K_alpha',format="$s K-alpha = $s")
Ti K-alpha = 2.7496
Cr K-alpha = 2.2909
Mn K-alpha = 2.1031
...
Ag K-alpha = 0.5608
```

### 1.4 Chemical Composition

Some properties are available for groups of elements. Groups are specified as a chemical formula string and either density or cell volume for the crystal structure. While it does not provide any information about molecular structure, a formula does all complete control over chemical composition.
• Individual atoms are represented by periodic table symbol. These are case sensitive, so “CO” is different from “Co”.

• Formula strings consist of counts and atoms such as “CaCO3+6H2O”.

• Groups can be separated by ‘+’ or space, so “CaCO3 + 6H2O” works as well.

• Groups can be defined using parentheses, such as “CaCO3 (H2O)6”.

• Parentheses can nest: “(CaCO3(H2O)6)1”.

• Isotopes are represented by index, e.g., “CaCO[18]3+6H2O”.

• Counts can be integer or decimal, e.g. “CaCO3+(3HO1.5)2”.

A formula string is translated into a formula using `periodictable.formula()`. Once the formula has been formed, you can perform algebra on the entire formula, such as adding together two formulas to make a more complex compound.

The following is an example of hydrated quartz:

```python
>>> import periodictable
>>> SiO2 = periodictable.formula('SiO2')
>>> hydrated = SiO2 + periodictable.formula('3H2O')
>>> print hydrated, 'mass', hydrated.mass
SiO2(H2O)3 mass 114.13014
>>> rho, mu, inc = periodictable.neutron_sld('SiO2+3H2O', density=1.5, wavelength=4.75)
>>> print hydrated, 'neutron sld', %.3g % rho
SiO2(H2O)3 neutron sld 0.849
>>> rho, mu = periodictable.xray_sld(hydrated, density=1.5, ...
... wavelength=periodictable.Cu.K_alpha)
>>> print hydrated, 'X-ray sld', %.3g % rho
SiO2(H2O)3 X-ray sld 13.5
```

Formulas are parsed from strings using the following grammar:

```
number :: [1-9][0-9] *
fraction :: ( | '0' | number) '.' [0-9]*
count :: number | fraction | ''
symbol :: [A-Z][a-z]*
isotope :: '[' number ']' | ''
element :: symbol isotope count
separator :: '+' | ''
group :: count element+ | '(' formula ')' count
grammar :: group separator formula | group | ''
```

### 1.5 Bundling with py2exe

When using periodictable as part of a bundled package, you need to be sure to include the data associated with the tables. This can be done by adding a periodictable entry into the `package_data` property of the distutils setup file:

```python
import periodictable
...
setup(..., package_data=periodictable.package_data, ...)
```

If you have a number of packages which add package data (for example, periodic table extensions), then you can use the following:

### 1.5. Bundling with py2exe
import periodictable

package_data = {}
...
package_data.update(periodictable.package_data)
...
setup(..., package_data=package_data, ...)

1.6 Adding properties

The periodic table is extensible. Third party packages can add attributes to the table, and they will appear in all of the elements.

In order to add a new property to the table, you need to define a python package which contains the required information, and can attach the information to the periodic table so that it is available on demand. This is done with the function `init` in your table extension.

This example adds the attribute `discoverer` to each element. First create the file `discoverer/core.py`:

""
Partial table of element discoverers.
""

import periodictable.core

def init(table, reload=False):
    if 'discoverer' in table.properties and not reload: return
    table.properties.append('discoverer')

    # Set the default, if any
    periodictable.core.Element.discoverer = "Unknown"

    # Not numeric, so no discoverer_units

    # Load the data
    for name,person in data.iteritems():
        el = table.name(name)
        el.discoverer = person

data = dict(
    arsenic="Jabir ibn Hayyan",
    antimony="Jabir ibn Hayyan",
    bismuth="Jabir ibn Hayyan",
    phosphorus="H. Brand",
    cobalt="G. Brandt",
    platinum="A. de Ulloa",
    nickel="A.F. Cronstedt",
    magnesium="J. Black",
)

Now that we have defined the `init` function, we need a way to call it. The simplest solution is to load it directly when your package is imported. In the current example, this could be done by adding the following line to the end of the file:
This would be fine for the current example because the table size is small and load time is fast. For large tables, you may wish to delay loading the table data until it is needed. To do this, we use the `periodictable.core.delayed_load()` function in our package `__init__` file `discoverer/__init__.py`:

```python
import periodictable.core

# Delayed loading of the element discoverer information

def _load_discoverer():
    """
    The name of the person or group who discovered the element.
    """
    from . import core
    core.init(periodictable.core.default_table())
    periodictable.core.delayed_load(['discoverer'], _load_discoverer)
```

The first argument to `delayed_load` is the list of all attributes that will be defined when the module is loaded. The second argument is the loading function, whose docstring will appear as the attribute description for each attribute in the first list.

Check that it works:

```python
>>> import discoverer
>>> import periodictable
>>> print(periodictable.magnesium.discoverer)
J. Black
```

Isotope and ion specific data is also supported. In this case we need a data table that contains information for each isotope of each element. The following example uses a dictionary of elements, with a dictionary of isotopes for each. It adds the `shells` attribute to Fe[56] and Fe[58].

Define `shelltable/core.py`:

```python
""
Example of isotope specific extensions to the periodic table.
""
from periodictable.core import Isotope

def init(table, reload=False):
    if 'shells' in table.properties and not reload: return
    table.properties.append('shells')

    # Set the default. This is required, even if it is only
    # setting it to None. If the attribute is missing then
    # the isotope data reverts to the element to supply the
    # value, which is almost certainly not what you want.
    Isotope.shells = None

    # Load the data
    for symbol, eldata in data.iteritems():
        el = table.symbol(symbol)
        for iso, isodata in eldata.iteritems():
            el[iso].shells = isodata
```

## 1.6. Adding properties
data = dict(
    Fe = {56: "56-Fe shell info",
          58: "58-Fe shell info"},
)

Again, we are going to initialize the table with delayed loading. In this case it is very important that we set the `isotope=True` keyword in the `delayed_load` call. If we don’t, then the magic we use to return the correct value after loading the new table information fails. Since unknown attributes are delegated to the underlying element, the value for the natural abundance will be returned instead. On subsequent calls the isotope specific value will be returned.

This is demonstrated in `shelltable/__init__.py`:

```python
import periodictable.core
# Delayed loading of the element discoverer information
def _load():
    ""
    The name of the person or group who discovered the element.
    ""
    from . import core
    core.init(periodictable.core.default_table())
    periodictable.core.delayed_load({'shells'}, _load,
                                   isotope=True, element=False)

Check that it works:

>>> import shelltable
>>> import periodictable
>>> print periodictable.Fe[56].shells
56-Fe shell info
>>> print periodictable.Ni[58].shells
None

Ion specific data is more complicated, particularly because of the interaction with isotopes. For example, `Ni[58].ion[3]` should have the same mass as `Ni[58]` (the mass of the electron is negligible), but a different mass from `Ni.ion[3]`. However, the f_0 scattering factors for X-rays are dependent on the ionization state, so `Ni[58].ion[3].xray.f0(Q)` and `Ni.ion[3].xray.f0(Q)` are the same but different from `Ni.xray.f0(Q)`.

Current support for ion dependent properties is awkward. The X-ray table `periodictable.xsf` creates a specialized structure for each ion as it is requested. The magnetic form factor table `periodictable.magnetic_ff` does not try to support `ion.magnetic_ff` directly, but instead the user must request `ion.magnetic_ff[ion.charge]`. Properties dependent on both isotope and ion can probably be implemented, but there are no examples yet.

Be sure to use the `ion=True` keyword for `delayed_load` when the table extension contains ion specific information.

## 1.7 Custom tables

You can create your own private instance of PeriodicTable and populate it with values.

Example:
>>> import periodictable
>>> from periodictable import core, mass, density, elements

>>> mytable = core.PeriodicTable(table="H=1")
>>> mass.init(mytable)
>>> density.init(mytable)

>>> # Reset mass to H=1 rather than C=12
>>> scale = elements.H[1].mass
>>> for el in mytable:
    ...  el._mass /= scale
    ...  if hasattr(el,'_density') and el._density != None:
    ...      el._density /= scale
    ...
    ...
    ...

>>> print mytable.H[1].mass, mytable.C[12].mass
1.0 11.9068286833
>>> print periodictable.H[1].mass, periodictable.C[12].mass
1.0078250321 12.0

You will need to add individual properties by hand for all additional desired properties using module.init(elements).

The table name (H=1 above) must be unique within the session. If you are pickling elements from a custom table, you must create a custom table of the same name before attempting to restore them. The default table is just a custom table with the name default.

Support for custom tables could be made much smoother by delegating all properties not defined in the custom table back to the base table, much like is currently done for Isotopes and Ions. That way you only need to replace the properties of interest rather than defining all new properties.

The alternative to using custom tables is to replace a dataset in the base table using e.g., custom_mass.init(elements, reload = True), where custom_mass is your own version of the periodic table values. Be aware, however, that this will have a global effect, changing the mass used by all packages, but you are strongly discouraged from doing so.

### 1.8 Data Sources

**Physical constants**  NIST Physics Laboratory - Constants, units and uncertainty

**Atomic and isotope mass**  NIST Physics Laboratory - Atomic weights and isotope composition

**Atomic density**  ILL Neutron Data Booklet


**Neutron scattering factors**  Atomic Institute for Austrian Universities

**X-ray scattering factors**  Center for X-Ray Optics

**Crystal structure**  Ashcroft and Mermin
1.9 License

This program is in the public domain.

1.10 Disclaimer

This data has been compiled from a variety of sources for the user’s convenience and does not represent a critical evaluation by the authors. While we have made efforts to verify that the values we use match published values, the values themselves are based on measurements whose conditions may differ from those of your experiment.

1.11 Credits

Periodictable was written by Paul Kienzle and is now developed and maintained by the DANSE project.

We are grateful for the existence of many fine open source packages such as Pyparsing, NumPy and Python without which this package would be much more difficult to write.
2.1 Core table

2.1.1 periodictable.core

Core classes for the periodic table.

- **PeriodicTable** The periodic table with attributes for each element.
  
  **Note:** PeriodicTable is not a singleton class. Use `periodictable.elements` to access the common table.

- **Element** Element properties such as name, symbol, mass, density, etc.

- **Isotope** Isotope properties such as mass, density and neutron scattering factors.

- **Ion** Ion properties such as charge.

Elements are accessed from a periodic table using `table[number], table.name or table.symbol` where `symbol` is the two letter symbol. Individual isotopes are accessed using `element[isotope]`. Individual ions are references using `element.ion[charge]`. There are presently no properties specific to both ion and isotope.

Helper functions:

- **delayed_load()** Delay loading the element attributes until they are needed.

- **get_data_path()** Return the path to the periodic table data files.

- **define_elements()** Define external variables for each element in namespace.

- **default_table()** Returns the common periodic table.

See Also:

*Adding properties* for details on extending the periodic table with your own attributes.

*Custom tables* for details on managing your own periodic table with custom values for the attributes.

```python
class Ion(element, charge):
    Bases: object

    Periodic table entry for an individual ion. An ion is associated with an element. In addition to the element properties (`symbol, name, atomic number`), it has specific ion properties (`charge`). Properties not specific to the ion (i.e., `charge`) are retrieved from the associated element.

    xray
        X-ray scattering properties for the elements.

```
class Isotope (element, isotope_number)
   Bases: object

   Periodic table entry for an individual isotope. An isotope is associated with an element. In addition to the element properties (symbol, name, atomic number), it has specific isotope properties (isotope number, nuclear spin, relative abundance). Properties not specific to the isotope (e.g., x-ray scattering factors) are retrieved from the associated element.

   abundance
      Natural abundance.
      Parameters isotope : Isotope
      Returns abundance : float |

density
   Element density for natural abundance. For isotopes, return the equivalent density assuming identical inter-atomic spacing as the naturally occurring material.
      Parameters
         iso_el [isotope or element] Name of the element or isotope.
      Returns density : float | g/cm^3
      Reference: ILL Neutron Data Booklet, original values from CRC Handbook of Chemistry and Physics, 80th ed. (1999).

mass
   Atomic weight.
      Parameters isotope : Isotope
      Returns
         mass [float | u] Atomic weight of the element.

neutron
   Neutron scattering factors, nuclear_spin and abundance properties for elements and isotopes.

class Element (name, symbol, Z, ions, table)
   Bases: object

   Periodic table entry for an element. An element is a name, symbol and number, plus a set of properties. Individual isotopes can be referenced as element[isotope_number]. Individual ionization states can be referenced by element.ion[charge].

   add_isotope (number)
      Add an isotope for the element.
      Parameters
         number [integer] Isotope number, which is the number protons plus neutrons.
      Returns None
**K_{alpha}**
X-ray emission lines for various elements, including Ag, Pd, Rh, Mo, Zn, Cu, Ni, Co, Fe, Mn, Cr and Ti. 
*K_{alpha} is the average of K_{alpha1} and K_{alpha2} lines.*

**K_{alpha_units}**
X-ray emission lines for various elements, including Ag, Pd, Rh, Mo, Zn, Cu, Ni, Co, Fe, Mn, Cr and Ti. 
*K_{alpha} is the average of K_{alpha1} and K_{alpha2} lines.*

**K_{beta1}**
X-ray emission lines for various elements, including Ag, Pd, Rh, Mo, Zn, Cu, Ni, Co, Fe, Mn, Cr and Ti. 
*K_{alpha} is the average of K_{alpha1} and K_{alpha2} lines.*

**K_{beta1_units}**
X-ray emission lines for various elements, including Ag, Pd, Rh, Mo, Zn, Cu, Ni, Co, Fe, Mn, Cr and Ti. 
*K_{alpha} is the average of K_{alpha1} and K_{alpha2} lines.*

**covalent_radius**
Add covalent_radius property to the elements.

*Note:* covalent radii data source is unknown.

**covalent_radius_uncertainty**
Add covalent_radius uncertainty property to the elements.

**covalent_radius_units**
Add covalent_radius_units property to the elements.

**crystal_structure**
Add crystal_structure property to the elements.

**density**
Element density for natural abundance. For isotopes, return the equivalent density assuming identical inter-atomic spacing as the naturally occuring material.

*Parameters*

iso_el [isotope or element] Name of the element or isotope.

*Returns* density : float | g/cm^3

*Reference:* *Ashcroft and Mermin.*

**interatomic_distance**
Estimated interatomic distance from atomic weight and density. The distance between isotopes is assumed to match that between atoms in the natural abundance.

*Parameters*

element [Element] Name of the element whose interatomic distance needs to be calculated.

*Returns* distance : float | A

Interatomic distance is computed using:

\[ d = \frac{\text{atomic weight}}{(\text{density} \times 0.602214179)}^{(1/3)}. \]

with units:

\[ \frac{(\text{g/mol})}{(\text{g/cm}^3 \text{ atoms/mol})} \times 10^8 \text{A/cm}^3^{(1/3)} = \text{A} \]
ionic_radius
   Ionic radii for various charges. These values are directly from CrysFML.

isotopes
   List of all isotopes

magnetic_ff
   Magnetic Form Factors. These values are directly from CrysFML.

mass
   Atomic weight.
   Parameters isotope: Isotope
   Returns
      mass [float | u] Atomic weight of the element.

neutron
   Neutron scattering factors, nuclear_spin and abundance properties for elements and isotopes.

number_density
   Estimate the number density from atomic weight and density. The density for isotopes is assumed to match that of between atoms in natural abundance.
   Parameters
      element [element] Name of the element whose number density needs to be calculated.
   Returns
      Nb [float | unitless] Number density of a element.

xray
   X-ray scattering properties for the elements.

class PeriodicTable (table='default')
   Bases: object
   Defines the periodic table of the elements with isotopes. Individual elements are accessed by name, symbol or atomic number. Individual isotopes are addressable by element[mass_number] or elements.isotope(element name), elements.isotope(element symbol).

For example, the following all retrieve iron:

>>> from periodictable import *
>>> print elements[26] # Fe
Fe
>>> print elements.Fe # Fe
Fe
>>> print elements.symbol('Fe') # Fe
Fe
>>> print elements.name('iron')
Fe

```python
>>> print elements.isotope('Fe')
Fe
```

To get iron-56, use:

```python
>>> print elements[26][56]
56-Fe
>>> print elements.Fe[56]
56-Fe
>>> print elements.isotope('56-Fe')
56-Fe
```

Deuterium and tritium are defined as ‘D’ and ‘T’. Some neutron properties are available in `elements[0]`.

To show all the elements in the table, use the iterator:

```python
>>> from periodictable import *
>>> for el in elements:  # lists the element symbols
...     print el.symbol,el.name
n neutron
H hydrogen
He helium
...
Uuh ununhexium
```

**Note:** Properties can be added to the elements as needed, including mass, nuclear and X-ray scattering cross sections. See section *Adding properties* for details.

**isotope**(input)

Lookup the element or isotope in the periodic table. Elements are assumed to be given by the standard element symbols. Isotopes are given by number-symbol, or ‘D’ and ‘T’ for 2-H and 3-H.

**Parameters**

- **input** [string] Element name or isotope to be looked up in periodictable.

**Returns** Element

**Raises** ValueError if element or isotope is not defined.

**Example** Print the element corresponding to ‘58-Ni’.

```python
>>> import periodictable
>>> print periodictable.elements.isotope('58-Ni')
58-Ni
```

**list**(props, **kw)

Print a list of elements with the given set of properties.

**Parameters**

- **props**, **kw** [string] Name of the properties to print

  **format:** string Template for displaying the element properties, with one % for each property.

**Returns** None

**Example** Print a table of mass and density.

---

2.1. Core table
>>> from periodictable import elements
>>> elements.list('symbol','mass','density', ...
    .format='%-2s: %6.2f u %5.2f g/cm^3')
H : 1.01 u 0.07 g/cm^3
He: 4.00 u 0.12 g/cm^3
Li: 6.94 u 0.53 g/cm^3
...
Bk: 247.00 u 14.00 g/cm^3

name (input)

Lookup an element given its name.

Parameters

input  [string] Element name to be looked up in periodictable.

Returns  Element

Raises  ValueError if element does not exist.

Example  Print the element corresponding to ‘iron’.

>>> import periodictable
>>> print periodictable.elements.name('iron')
Fe

symbol (input)

Lookup the an element in the periodic table using its symbol. Symbols are included for ‘D’ and ‘T’, deuterium and tritium.

Parameters

input  [string] Element symbol to be looked up in periodictable.

Returns  Element

Raises  ValueError if the element symbol is not defined.

Example  Print the element corresponding to ‘Fe’.

>>> import periodictable
>>> print periodictable.elements.symbol('Fe')
Fe

delayed_load (all_props, loader, element=True, isotope=False, ion=False)

Delayed loading of an element property table. When any of property is first accessed the loader will be called to load the associated data. The help string starts out as the help string for the loader function. The attribute may be associated with any of Isotope, Ion, or Element. Some properties, such as mass, have both an isotope property for the mass of specific isotopes, as well as an element property for the mass of the collection of isotopes at natural abundance. Set the keyword flags element, isotope and/or ion to specify which of these classes will be assigned specific information on load.

define_elements (table, namespace)

Define external variables for each element in namespace. Elements are defined both by name and by symbol.

This is called from __init__ as:

    elements = core.default_table()
    __all__ += core.define_elements(elements, globals())
Parameters

  *table* [PeriodicTable] Set of elements
  
  *namespace* [dict] Namespace in which to add the symbols.
  
Returns [string, ...] A sequence listing the names defined.

Note: This will only work for the namespace globals(), not locals()!

**get_data_path** *(data)*

Locate the directory for the tables for the named extension.

Parameters

  *data* [string] Name of the extension data directory. For example, the xsf extension has data in
  the ‘xsf’ data directory.

Returns string Path to the data.

**default_table** *(table=None)*

Return the default table unless a specific table has been requested.

This is to be used in a context like:

```python
def summary(table=None):
    table = core.default_table(table)
    ...
```

### 2.2 Chemical formula operations

#### 2.2.1 periodictable.formulas

Chemical formula parser.

**class Formula** *(value=None, density=None, name=None)*

Bases: object

Simple chemical formula representation. This is designed for calculating molar mass and scattering length density, not for representing bonds or atom positions. We preserve the structure of the formula so that it can be used as a basis for a rich text representation such as matplotlib TeX markup.

Parameters

  *formula* [see below] Chemical formula.
  
  *density* [float | g/cm**3] Material density.
  
  *name* [string] Common name for the molecule.

Exceptions *ValueError* : invalid formula initializer

Formula initializers can have a variety of forms:

- **string**: `m = Formula( “CaCO3+6H2O” )`
  
  For full details see *Formula grammar*

- **structure**: `m = Formula( [(1,Ca),(2,C),(3, O),(6,[(2,H),(1,O)])] )`

- **formula math**: `m = Formula( “CaCO3” ) + 6*Formula( “H2O” )`

- **another formula (makes a copy)**: `m = Formula( Formula(“CaCO3+6H2O”))`
an atom: \( m = \text{Formula(Ca)} \)

nothing: \( m = \text{Formula()} \)

**neutron\_sld** (*wavelength=1*)

Neutron scattering information for the molecule.

**Parameters**

\[
\text{wavelength} \quad \text{[float | A]} \quad \text{Wavelength of the neutron beam.}
\]

**Returns** sld : (float, float, float) \( \text{10}^{-6} \text{ inv A}^2 \)

Neutron scattering length density is returned as the tuple \((\text{real, imaginary, incoherent})\), or as \((\text{None, None, None})\) if the mass density is not known.

**volume** (*packing\_factor='hcp'*)

Estimate molecular volume.

The crystal volume can be estimated from the element covalent radius and the atomic packing factor using:

\[
\text{packing\_factor} = \text{N\_atoms V\_atom / V\_crystal}
\]

Packing factors for a number of crystal lattice structures are defined.

**Table 2.1: Crystal lattice names and packing factors**

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
<th>Formula</th>
<th>Packing factor</th>
</tr>
</thead>
<tbody>
<tr>
<td>cubic</td>
<td>simple cubic</td>
<td>( \pi \ 1/6 )</td>
<td>0.52360</td>
</tr>
<tr>
<td>bcc</td>
<td>body-centered cubic</td>
<td>( \pi \ \sqrt{3}/8 )</td>
<td>0.68017</td>
</tr>
<tr>
<td>hcp</td>
<td>hexagonal close-packed</td>
<td>( \pi \ \sqrt{3}/18 )</td>
<td>0.74048</td>
</tr>
<tr>
<td>fcc</td>
<td>face-centered cubic</td>
<td>( \pi \ \sqrt{3}/18 )</td>
<td>0.74048</td>
</tr>
<tr>
<td>diamond</td>
<td>diamond cubic</td>
<td>( \pi \ \sqrt{3}/16 )</td>
<td>0.34009</td>
</tr>
</tbody>
</table>

**Parameters**

\[
\text{packing\_factor} = \text{‘hcp’} \quad \text{[float or string]} \quad \text{Atomic packing factor. If packing\_factor is the name of a crystal lattice, use the lattice packing factor.}
\]

**Returns** volume : float \( \text{A}^3 \) Molecular volume.

**Raises** ValueError : lattice is not defined

**xray\_sld** (*energy=None, wavelength=None*)

X-ray scattering length density for the molecule.

**Parameters**

\[
\text{energy} \quad \text{[float | keV]} \quad \text{Energy of atom.}
\]

\[
\text{wavelength} \quad \text{[float | A]} \quad \text{Wavelength of atom.}
\]

**Returns** sld : (float, float) \( \text{inv A}^2 \) X-ray scattering length density is return as the tuple \((\text{real, imaginary})\), or as \((\text{None, None})\) if the mass density is not known.

**atoms**

\{ atom: count, ... \}

Composition of the molecule. Referencing this attribute computes the count as the total number of each element or isotope in the chemical formula, summed across all subgroups.
hill

Formula

Convert the formula to a formula in Hill notation. Carbon appears first followed by hydrogen then the remaining elements in alphabetical order.

mass

atomic mass units u (C\[12\] = 12 u)

Atomic mass of the molecule.

Referencing this attribute computes the mass of the chemical formula.

**formula_grammar**(table=None)

Construct a parser for molecular formulas.

**Parameters**

- **table**: [PeriodicTable] If table is specified, then elements and their associated fields will be chosen from that periodic table rather than the default.

**Returns**

* parser : pyparsing.ParserElement The parser.parseString() method returns a list of pairs (count, fragment), where fragment is an isotope, an element or a list of pairs (count, fragment).

### 2.3 Covalent radius

#### 2.3.1 periodictable.covalent_radius

This module adds the following fields to the periodic table

- covalent_radius
- covalent_radius_uncertainty
- covalent_radius_units = ‘angstrom’

Use **init()** to initialize a private table.

Data is taken from Cordero 2008 \(^1\). The abstract of this paper reads as follows:

A new set of covalent atomic radii has been deduced from crystallographic data for most of the elements with atomic numbers up to 96. The proposed radii show a well behaved periodic dependence that allows us to interpolate a few radii for elements for which structural data is lacking, notably the noble gases. The proposed set of radii therefore fills most of the gaps and solves some inconsistencies in currently used covalent radii. The transition metal and lanthanide contractions as well as the differences in covalent atomic radii between low spin and high spin configurations in transition metals are illustrated by the proposed radii set.

**Notes:**

1. Values are averages only. The particular radius can be highly dependent on oxidation state and chemical compound.
2. The paper lists values for multiple spin states on select elements. We are using sp\(^3\) for carbon and low spin for manganese, iron and cobalt.
3. Elements with zero or one measurements of covalent radius are assigned an uncertainty of 0.00. These are He, Ne, Pm, At, Rn, Fr, Ac, Pa.

4. Elements above 96 are assigned a covalent radius and uncertainty of None.

5. Radii are measured from bonds to C, N or O. The choice of which compound was used is element dependent. Details are available in the references.

\texttt{init}(\texttt{table, reload=False})

Add the covalent radius property to a private table. Use \texttt{reload = True} to replace the covalent radius property on an existing table.

### 2.4 Crystal structure

#### 2.4.1 \texttt{periodictable.crystal\_structure}

Crystal structure data.

Adds \texttt{crystal\_structure} to the periodic table. Each crystal structure is a dictionary which contains the key ‘symmetry’. Depending on the value of \texttt{crystal\_structure[‘symmetry’]}, one or more parameters ‘a’, ‘c/a’, ‘b/a’, ‘d’, and ‘alpha’ may be present according to the following table:

<table>
<thead>
<tr>
<th>Symmetry</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>atom</td>
<td>d</td>
</tr>
<tr>
<td>diatom</td>
<td>a</td>
</tr>
<tr>
<td>BCC</td>
<td>c/a, a</td>
</tr>
<tr>
<td>fcc</td>
<td>a</td>
</tr>
<tr>
<td>hcp</td>
<td>a</td>
</tr>
<tr>
<td>Tetragonal</td>
<td>c/a, a</td>
</tr>
<tr>
<td>Cubic</td>
<td>a</td>
</tr>
<tr>
<td>Diamond</td>
<td>a</td>
</tr>
<tr>
<td>Orthorhombic</td>
<td>c/a, a, b/a</td>
</tr>
<tr>
<td>Rhombohedral</td>
<td>a, alpha</td>
</tr>
<tr>
<td>SC</td>
<td>a</td>
</tr>
<tr>
<td>Monoclinic</td>
<td>alpha</td>
</tr>
</tbody>
</table>

Example:

```python
>>> import periodictable as elements
>>> print elements.C.crystal_structure[‘symmetry’]
Diamond
>>> print elements.C.crystal_structure[‘a’]
3.57
```

This data is from Ashcroft and Mermin.

\texttt{init}(\texttt{table, reload=False})

### 2.5 Density

#### 2.5.1 \texttt{periodictable\_density}

The following properties are added:
• density
• **density_units (g/cm³)** Densities for solids and liquids are given as specific gravities at 20 C unless other wise indicated by **density_caveat**. Densities for gaseous elements are given for the liquids at their boiling points. Missing data are represented by **None**.

• **density_caveat** Comments on the density, if not taken in standard conditions.
• interatomic_distance
• **interatomic_distance_units (angstrom)** Interatomic distance estimated from element density.
• number_density
• **number_density_units (unitless)** Number density estimated from mass and density.

Density for the isotope is computed assuming that the atomic spacing is the same as that for the element in the natural abundance.

```python
>>> from periodictable import D, H
>>> print "H :", H.density,", D :", D.density
H : 0.0708 , D : 0.141475093639
>>> print (D.density/H.density) / (D.mass/H.mass)
1.0
```

The following plot shows density for all elements:

![Density for elements](image)

2.5. Density
From the X-ray data book: http://xdb.lbl.gov/Section5/Sec_5-2.html
Data were taken mostly from ². These values are reproduced in ³.

density (iso_el)
Element density for natural abundance. For isotopes, return the equivalent density assuming identical inter-
atomic spacing as the naturally occurring material.

Parameters

  iso_el [isotope or element] Name of the element or isotope.

Returns density : float | g/cm³

Reference: ILL Neutron Data Booklet, original values from CRC Handbook of Chemistry and Physics, 80th

init (table, reload=False)

interatomic_distance (element)
Estimated interatomic distance from atomic weight and density. The distance between isotopes is assumed to
match that between atoms in the natural abundance.

Parameters

  element [Element] Name of the element whose interatomic distance needs to be calculated.

Returns distance : float | Å

Interatomic distance is computed using:

d = atomic_weight/(density*0.602214179)^(1/3).

with units:

((g/mol)/(g/cm³)(atoms/mol))(10^8Å/cm^3)^(1/3) = Å

number_density (element)
Estimate the number density from atomic weight and density. The density for isotopes is assumed to match that
of between atoms in natural abundance.

Parameters

  element [element] Name of the element whose number density needs to be calculated.

Returns

  Nb [float | unitless] Number density of an element.

2.6 Mass

2.6.1 periodictable.mass

Adds average mass for the elements:

- mass
- mass_units ('u') The atomic mass averaged over natural abundances.

Periodic Table Documentation, Release 0.9

Adds mass and abundance information for isotopes:

- **mass**
- **mass_units** (*u*) The individual isotope mass.
- **abundance**
- **abundance_units** (*%*) Natural abundance for the isotope.

Atomic Weights and Isotopic Composition

The atomic weights are available for elements 1 through 112, 114, & 116 and isotopic compositions or abundances are given when appropriate. The atomic weights data were published by Coplen \(^4\) in Atomic Weights of the Elements 1999, (and include changes reported from the 2001 review in Chem. Int., 23, 179 (2001)) and the isotopic compositions data were published by Rosman \(^6\) and Taylor \(^7\) in Isotopic Compositions of the Elements 1997. The relative atomic masses of the isotopes data were published by Audi \(^8\) and Wapstra \(^9\) in the 1995 Update To The Atomic Mass Evaluation.

This data has been compiled from the above sources for the user’s convenience and does not represent a critical evaluation by the NIST Physics Laboratory. [http://physics.nist.gov/PhysRefData/Compositions/](http://physics.nist.gov/PhysRefData/Compositions/)


**abundance**(isotope)

Natural abundance.

**Parameters** isotope : Isotope

**Returns** abundance : float |


**getval**(str)

**init**(table, reload=False)

**mass**(isotope)

Atomic weight.

**Parameters** isotope : Isotope

**Returns** mass [float | u] Atomic weight of the element.


### 2.7 Neutron scattering potentials

#### 2.7.1 periodictable.nsf

Neutron scattering factors for the elements and isotopes.

---


\(^5\) Coplen. T. B.: U.S. Geological Survey, Reston, Virginia, USA.

\(^6\) Rosman. K. J. R.: Department of Applied Physics, Curtin University of Technology, Australia.


\(^8\) Audi. G.: Centre de Spectrométrie Nucléaire et de Spectrométrie de Masse, Orsay Campus, France.

For details of neutron scattering factor values, see `Neutron`. The property is set to `None` if there is no neutron scattering information for the element. Individual isotopes may have their own scattering information.

**Example**

Print a table of coherent scattering length densities for isotopes of a particular element:

```python
>>> import periodictable
>>> for iso in periodictable.Ni:
...     if iso.neutron.has_sld():
...         print iso,iso.neutron.sld()[0]
58-Ni 13.152605395
60-Ni 2.55745104902
61-Ni 6.94165284735
62-Ni -7.94636575947
64-Ni -0.337948888621
```

**Details**

There are a number of functions available in `periodictable.nsf`

- `neutron_energy()` Return energy given wavelength.
- `neutron_wavelength()` Return wavelength given energy.
- `neutron_scattering()` Computes SLD, cross sections and penetration depth for a compound.
- `neutron_sld()` Computes SLD for a compound.
- `energy_dependent_table()` Lists energy dependent isotopes.
- `sld_table()` Lists all elements in natural abundance.
- `absorption_comparison_table()` Compares `element.neutron.b_c_i` and `element.neutron.absorption`.
- `coherent_comparison_table()` Compares `element.neutron.b_c` and `element.neutron.coherent`.
- `total_comparison_table()` Compares `element.neutron.b_c` and `element.neutron.coherent`.

For private tables use `init()` to set the data.

The neutron scattering information table is reproduced from the Atomic Institute for Austrian Universities (2007 version):

http://www.ati.ac.at/~neutropt/scattering/table.html

The above site has references to the published values for every entry in the table. We have included these in the documentation directory associated with the `periodictable` package.

**References**

```python
class Neutron()
    Bases: object
```

Neutron scattering factors are attached to each element in the periodic table for which values are available. If no information is available, then the neutron field of the element will be `None`. Even when neutron information is available, it may not be complete, so individual fields may be `None`.

The following fields are used:
• **b_c (fm)** Bounds coherent scattering length.

• **b_c_i (fm)** Imaginary part of bound coherent scattering length. This is related to absorption cross section by \(2\pi k/k\) where \(k = 2\pi/\lambda\) with a factor of 100 for converting between barns and fm. \(b_c_i\) is not available for all isotopes for which absorption cross sections have been measured.

• **bp,bm (fm)** Spin-dependent scattering for I+1/2 and I-1/2 (not always available). Incoherent scattering arises from the spin-dependent scattering \(b_+\) and \(b_-\). The Neutron Data Booklet \(^\text{10}\) gives formulas for calculating coherent and incoherent scattering from \(b_+\) and \(b_-\) alone.

• **bp_i,bm_i (fm)** Imaginary portion. See the Neutron Data Booklet \(^1\) for details.

• **is_energy_dependent (boolean)** Do not use this data if scattering is energy dependent.

• **coherent (barns)** Coherent scattering cross section. In theory coherent scattering is related to bound coherent scattering by \(4\pi b_c^2/100\). In practice, these values are different, with the following table showing the largest relative difference:

<table>
<thead>
<tr>
<th>Element</th>
<th>Difference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sc</td>
<td>3%</td>
</tr>
<tr>
<td>Ti</td>
<td>4%</td>
</tr>
<tr>
<td>V</td>
<td>34%</td>
</tr>
<tr>
<td>Mn</td>
<td>1%</td>
</tr>
<tr>
<td>Cd</td>
<td>4%</td>
</tr>
<tr>
<td>Te</td>
<td>4%</td>
</tr>
<tr>
<td>Xe</td>
<td>9%</td>
</tr>
<tr>
<td>Sm</td>
<td>100%</td>
</tr>
<tr>
<td>Eu</td>
<td>46%</td>
</tr>
<tr>
<td>Gd</td>
<td>61%</td>
</tr>
<tr>
<td>Tb</td>
<td>1%</td>
</tr>
<tr>
<td>Ho</td>
<td>11%</td>
</tr>
<tr>
<td>W</td>
<td>4%</td>
</tr>
<tr>
<td>Hg</td>
<td>2%</td>
</tr>
</tbody>
</table>

• **incoherent (barns)** Incoherent scattering cross section.

• **total (barns)** Total scattering cross section. This is just coherent+incoherent.

• **absorption (barns)** Absorption cross section at 1.798 angstroms. Scale to your beam by dividing by \(\text{periodictable.nsf.ABSORPTION_WAVELENGTH}\) and multiplying by your wavelength.

For elements, the scattering cross-sections are based on the natural abundance of the individual isotopes. Individual isotopes may have additional information as follows:

<table>
<thead>
<tr>
<th>Property</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>abundance(%)</td>
<td>Abundance used in elemental measurements.</td>
</tr>
</tbody>
</table>

Each field above has a corresponding \_*_ units attribute with the name of the units. For scattering calculations, the scattering length density is the value of interest. This is computed from the number_density of the individual elements, as derived from the element density and atomic mass.

**Note:** 1 barn = 100 fm^2

**has_sld()**

Returns True if sld is defined for this element/isotope.

**scattering**(wavelength=1.798, energy=None)

Returns neutron scattering information for the element at natural abundance and density.

**Warning:** Incoherent SLD values have not been verified.

**Parameters**

- **wavelength** : float | A

**Returns**

- *sld* [(float, float, float) | 10^-6 / A^2] (real, imaginary, incoherent) scattering length density
- *xs* [(float, float, float) | 1/cm] (coherent, absorption, incoherent) cross sections.
- *penetration* [float | cm] 1/e penetration length.

**Algorithm**


### 2.7. Neutron scattering potentials

---

---
See `neutron_scattering()` for details.

**sld** *(wavelength=1.798, energy=None)*  
Returns scattering length density for the element at natural abundance and density.

**Warning:** Incoherent SLD values have not been verified.

**Parameters**  
**wavelength** : float | A

**Returns**  
**sld** [(float, float, float) | 10^-6 / A^2] (real, imaginary, incoherent) scattering length density.

**Algorithm**

See `neutron_scattering()` for details.

**init** *(table, reload=False)*  
Loads the Rauch table from the neutron data book.

**neutron_energy** *(wavelength)*  
Convert neutron wavelength to energy.

**Parameters**  
**wavelength** : float or vector | A

**Returns**  
**energy** : float or vector | meV

**Algorithm**  
\[ E = \frac{1}{2} m \, v^2 = \frac{\hbar^2}{2 \, m \, \lambda^2} \]  
\[ \hbar = \text{planck's constant in J s m} = \text{neutron mass in kg} \]

**neutron_wavelength** *(energy)*  
Convert neutron energy to wavelength.

**Parameters**  
**energy** : float or vector | meV

**Returns**  
**wavelength** : float or vector | A

**Algorithm**  
\[ E = \frac{1}{2} m \, v^2 = \frac{\hbar^2}{2 \, m \, \lambda^2} \]  
\[ \lambda = \sqrt{\frac{\hbar^2}{2 \, m \, E}} \]  
\[ \hbar = \text{planck's constant in J s m} = \text{neutron mass in kg} \]

**neutron_scattering** *(compound, density=None, wavelength=1.798, energy=None)*  
Computes neutron scattering cross sections for molecules.

**Warning:** Incoherent SLD values have not been verified.

**Parameters**

**compound** [Formula initializer] Chemical formula  
**density** [float | g/cm³] Mass density  
**wavelength** 1.798 [float | A] Neutron wavelength.  
**energy** [float | meV] Neutron energy. If energy is specified then wavelength is ignored.

**Returns**

**sld** [(float, float, float) | 10^-6 / A^2] (real, imaginary, incoherent) scattering length density.  
**xs** [(float, float, float) | 1/cm] (coherent, absorption, incoherent) cross sections.  
**penetration** [float cm] 1/e penetration length of the beam
Raising `AssertionError`: density is missing.

The coherent and incoherent cross sections are calculated from the bound scattering lengths for nuclei. The actual cross sections depend on the incoming neutron energy and sample temperature, especially for light elements. For low energy neutrons (cold neutrons), the tabulated cross sections are generally a lower limit. The measured incoherent scattering from hydrogen, for example, can be considerably larger (by more than 20%) than its bound value. For example, the incoherent scattering cross section of H2O is 5.621/cm as computed from these tables compared to ~7.0/cm as measured with 5 meV neutrons at 290K. 11

The scattering factor tables are not self consistent. The following functions show discrepancies between the various measurements of the scattering potential:

```python
absorption_comparison_table()
coherent_comparison_table()
total_comparison_table()
```

Algorithm

We first need to average quantities for the unit cell of the molecule.

Molecular weight $m$ (g/mol) is the sum of the weights of each component:

$$m = \sum n_i m_i \text{ for each atom } i = 1, 2, \ldots$$  \hspace{1cm} (2.1)

Cell volume $V$ (Å³/molecule) is molecular weight $m$ over density $\rho$, with a correction for units based on Avogadro’s number $N_A$ (atoms/mol) and the length conversion 1e8 Å/cm:

$$V = m/\rho 1 / N_A (10^8)^3$$ \hspace{1cm} (2.2)

Number density $N$ is the number of scatterers per unit volume:

$$N = \sum n_i / V$$ \hspace{1cm} (2.3)

Coherent scattering cross section $\sigma_c$ of the molecule is computed from the average scattering length of its constituent atoms, weighted by their frequency.

$$b_c = \sum n_i \text{Im}(b_c) / \sum n_i$$ \hspace{1cm} (2.4)

This is converted to a scattering cross section and scaled by 1 barn = 100 fm²:

$$\sigma_c = 4\pi b_c^2 / 100$$ \hspace{1cm} (2.5)

Similarly, the absorption cross section $\sigma_a$ and the total cross section $\sigma_s$ can be computed from the corresponding cross sections of the constituent elements, already expressed in barns:

$$\sigma_a = \sum n_i \sigma_{ai} / \sum n_i$$ \hspace{1cm} (2.6)

and

$$\sigma_s = \sum n_i \sigma_{si} / \sum n_i$$ \hspace{1cm} (2.7)

The total cross section is just the coherent plus incoherent cross sections:

$$\sigma_i = \sigma_s - \sigma_c$$ \hspace{1cm} (2.8)

---

The absorption cross sections are tabulated at wavelength 1.798 Å. In the thermal neutron energy range the absorption cross section is assumed to scale linearly with wavelength, and can be adjusted with a simple multiplication:

\[ \sigma_a = \sigma_a \frac{\lambda}{\lambda_0} = \sigma_a \frac{\lambda}{1.798} \quad (2.9) \]

For the scattering equations, the primary quantity of interest is the scattering potential \( b = b_p + i b_pp \). For most elements, the scattering potential at cold neutron and thermal neutron energies is simply related to the neutron energy, with no change in the real portion and a linear scaling of the imaginary portion with energy. The value of \( b \) is dominated by the bound coherent potential, with a small contribution from the incoherent scattering cross sections.

The potentials are related to the scattering cross sections as follows:

\[ \sigma_c = 4\pi |b_c|^2 \quad (2.10) \]
and

\[ \sigma_a = 4\pi b''/k \text{ for } k = 2\pi/\lambda \quad (2.11) \]

and

\[ \sigma_i = 4\pi |b_i|^2 \quad (2.12) \]

Transforming these we get:

\[ b' = b_c \quad (2.13) \]
and

\[ b'' = \sigma_a/(2\lambda) \quad (2.14) \]

and

\[ b_{inc} = \sqrt{\sigma_i/(4\pi)} \quad (2.15) \]

The incoherent potential \( b_{inc} \) can be treated primarily as an absorption potential in large scale structure calculations, with the complex potential \( b \) approximated by \( b_p + i (b_pp + b_{inc}) \).

The scattering potential is usually expressed as a scattering length density for calculation purposes. This is just the number density of the scatterers times their scattering potential:

\[ \rho_{re} = N b_c \quad (2.16) \]

and

\[ \rho_{im} = N \sigma_a/(2\lambda) \quad (2.17) \]
and

\[ \rho_{inc} = N \sqrt{\sigma_i/4\pi} \quad (2.18) \]

Scattering cross section:

\[ \Sigma_{coh} = N \sigma_c \quad (2.19) \]

and

\[ \Sigma_{inc} = N \sigma_i \quad (2.20) \]

and

\[ \Sigma_{abs} = N \sigma_a \quad (2.21) \]

1/e penetration depth \( d \):

\[ d = 1/(\Sigma_{coh} + \Sigma_{inc} + \Sigma_{abs}) \quad (2.22) \]

Including unit conversion with \( u = 10^{-6} \), the full equations are:

\[ \rho_{re} \, u/2 = (N/3) \left( b_c \, \text{fm} \right) \left( 10^{-5} / \text{fm} \right) \left( 10^6 \, u \right) \quad (2.23) \]

\[ ^{12} \text{Lynn, J.E. and Seeger, P.A. (1990) Resonance effects in neutron scattering lengths of rare-earth nuclides. Atomic Data and Nuclear Data Tables 44, 191-207.} \]

and
\[ \rho_{\text{im}} u^2 = \left( \frac{N}{A^3} \right) \left( \sigma_a \text{ barn} \right) \left( 10^{-8} \text{ barn} \right) \left( 2\lambda \right) \left( 10^6 \text{ u} \right) \] (2.24)

and
\[ \rho_{\text{inc}} u^2 = \left( \frac{N}{A^3} \right) \sqrt{\left( \frac{\sigma_i \text{ barn}}{4\pi} \right) \left( 100 \text{ fm}^2 \text{ barn} \right) \left( 10^{-5} \text{ fm} \right) \left( 10^6 \text{ u} \right)} \] (2.25)

and
\[ \Sigma_{\text{coh}} 1/\text{cm} = \left( \frac{N}{A^3} \right) \left( \sigma_c \text{ barn} \right) \left( 10^{-8} \text{ barn} \right) \left( 10^8 \text{ /cm} \right) \] (2.26)

and
\[ \Sigma_{\text{inc}} 1/\text{cm} = \left( \frac{N}{A^3} \right) \left( \sigma_i \text{ barn} \right) \left( 10^{-8} \text{ barn} \right) \left( 10^8 \text{ /cm} \right) \] (2.27)

and
\[ \Sigma_{\text{abs}} 1/\text{cm} = \left( \frac{N}{A^3} \right) \left( \sigma_a \text{ barn} \right) \left( 10^{-8} \text{ barn} \right) \left( 10^8 \text{ /cm} \right) \] (2.28)

and
\[ d \text{ cm} = \frac{1}{\left( \Sigma_{\text{coh}} 1/\text{cm} + \Sigma_{\text{inc}} 1/\text{cm} + \Sigma_{\text{abs}} 1/\text{cm} \right)} \] (2.29)

**neutron_sld(*args, **kw)**
Computes neutron scattering length densities for molecules.

**Warning:** Incoherent SLD values have not been verified.

### Parameters
- **compound** [Formula initializer] Chemical formula
- **density** [float | g/cm^3] Mass density
- **wavelength** [float | Å] Neutron wavelength.
- **energy** [float | meV] Neutron energy. If energy is specified then wavelength is ignored.

### Returns
- **sld** [(float, float, float) | 10^-6 / Å^2] (real, imaginary, incoherent) scattering length density.

**Raises** `AssertionError`: density is missing.

Returns the scattering length density of the compound. See `neutron_scattering()` for details.

**sld_plot(table=None)**
Plots SLD as a function of element number.

### Parameters
- **table** [PeriodicTable] The default periodictable unless a specific table has been requested.

### Returns None

**absorption_comparison_table(table=None, tol=None)**
Prints a table of $10^8 b_{c_i}$ and $-0.01*\text{absorption}/(2)(1.798)$ for each isotope where $b_{c_i}$ exists. This is used to checking the integrity of the data and formula.

The factor of 1.798 is the neutron wavelength at which the absorption is tallied. The factor of 0.01 transforms from barn/Å^3*1/Å to 10^-6/Å^2. The factor of 10 transforms from fm/Å^3 to 10^-6/Å^2.

### Parameters
- **table** [PeriodicTable] The default periodictable unless a specific table has been requested.
- **tol** 1e-3: float Show differences greater than this amount.

### Returns None

2.7. Neutron scattering potentials
coherent_comparison_table (table=None, tol=None)
Prints a table of $4*\pi*b_c^2/100$ and coherent for each isotope. This is useful for checking the integrity of the data and formula.

The table only prints where $b_c$ exists.

Parameters
- **table** [PeriodicTable] The default periodictable unless a specific table has been requested.

Returns None

incoherent_comparison_table (table=None, tol=None)
Prints a table of incoherent computed from total and $b_c$ with incoherent.

Parameters
- **table** [PeriodicTable] The default periodictable unless a specific table has been requested.

Returns None

total_comparison_table (table=None, tol=None)
Prints a table of neutron.total and sum coh,inc for each isotope where these exist. This is used to checking the integrity of the data and formula.

Parameters
- **table** [PeriodicTable] The default periodictable unless a specific table has been requested.

Returns None

energy_dependent_table (table=None)
Prints a table of energy dependent isotopes.

Parameters
- **table** [PeriodicTable] If table is not specified, use the common periodic table.

Returns None

sld_table (wavelength=1, table=None, isotopes=True)
Scattering length density table for wavelength 4.75 Å.

Parameters
- **table** [PeriodicTable] If table is not specified, use the common periodic table.
- **isotopes** = True [boolean] Whether to consider isotopes or not.

Returns None

neutron_sld_from_atoms (*args, **kw)
Deprecated since version 0.91: neutron_sld() now accepts dictionaries of {atom: count} directly.

2.8 X-ray scattering potentials

2.8.1 periodictable.xsf

This module has one class and nine functions.

Xray X-ray scattering properties for the elements.
The following attributes are added to each element:
Xray.sftable() Three column table of energy vs. scattering factors f1, f2.

Xray.scattering_factors() Returns f1, f2, the X-ray scattering factors for the given wavelengths interpolated from sftable.

Xray.f0() Returns f0 for the given vector Q, with q_i in [0,24pi] inv Ang.

Xray.sld() Returns scattering length density (real, imaginary) for the given wavelengths or energies.

The following functions are available for X-ray scattering information processing:

xray_wavelength() Finds X-ray wavelength in angstroms given energy in keV.

xray_energy() Finds X-ray energy in keV given wavelength in angstroms.

init() Initializes a periodic table with the Lawrence Berkeley Laboratory Center for X-Ray Optics xray scattering factors.

init_spectral_lines() Sets the K_alpha and K_beta1 wavelengths for select elements.

slp_table() Prints the xray SLD table for the given wavelength.

xray_sld() Computes xray scattering length densities for molecules.

xray_sld_from_atoms() The underlying scattering length density calculator. This works with a dictionary of atoms and quantities directly.

emission_table() Prints a table of emission lines.

K_alpha, K_beta1 (Angstrom): X-ray emission lines for various elements, including Ag, Pd, Rh, Mo, Zn, Cu, Ni, Co, Fe, Mn, Cr and Ti. K_alpha is the average of K_alpha1 and K_alpha2 lines.

X-ray scattering factors: Low-Energy X-ray Interaction Coefficients: Photoabsorption, scattering and reflection for E in 30 to 30,000 eV, and Z in 1 to 92.

Note: For custom tables, use init() and init_spectral_lines() to set the data.

X-ray f1 and f2 tables

The data for the tables is stored in the periodictable/xsf. directory. The following information is from periodictable/xsf/read.me, with minor formatting changes. These [nff] files were used to generate the tables published in reference 14. The files contain three columns of data:

Energy(eV), f_1, f_2,

where f_1 and f_2 are the atomic (forward) scattering factors. There are 500+ points on a uniform logarithmic mesh with points added 0.1 eV above and below “sharp” absorption edges. The tabulated values of f_1 contain a relativistic, energy independent, correction given by:

\[ Z^* = Z - (Z/82.5)^{2.37}. \]

Note: Below 29 eV f_1 is set equal to -9999.

The atomic photoabsorption cross section, \(\mu_a\), may be readily obtained from the values of f_2 using the relation:

\[ \mu_a = 2*r_0*\lambda*f_2 \]

where \(r_0\) is the classical electron radius, and \(\lambda\) is the wavelength. The index of refraction for a material with \(N\) atoms per unit volume is calculated by:

\[ \mu_a = 2*r_0*\lambda*f_2 \]

Note: Below 29 eV f_1 is set equal to -9999.

The atomic photoabsorption cross section, \(\mu_a\), may be readily obtained from the values of f_2 using the relation:

\[ \mu_a = 2*r_0*\lambda*f_2 \]

where \(r_0\) is the classical electron radius, and \(\lambda\) is the wavelength. The index of refraction for a material with \(N\) atoms per unit volume is calculated by:

These (semi-empirical) atomic scattering factors are based upon photoabsorption measurements of elements in their elemental state. The basic assumption is that condensed matter may be modeled as a collection of non-interacting atoms. This assumption is in general a good one for energies sufficiently far from absorption thresholds. In the threshold regions, the specific chemical state is important and direct experimental measurements must be made.

These tables are based on a compilation of the available experimental measurements and theoretical calculations. For many elements there is little or no published data and in such cases it was necessary to rely on theoretical calculations and interpolations across Z. In order to improve the accuracy in the future considerably more experimental measurements are needed.

Please send any comments about the tables to EMGullikson@lbl.gov.

Table 2.3: Note that the following elements have been updated since the publication of Ref. 1 in July 1993.

<table>
<thead>
<tr>
<th>Element</th>
<th>Updated</th>
<th>Energy Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg</td>
<td>1/15/94</td>
<td>30-50 eV</td>
</tr>
<tr>
<td>Al</td>
<td>1/15/94</td>
<td>30-73 eV</td>
</tr>
<tr>
<td>Si</td>
<td>1/15/94</td>
<td>30-100 eV</td>
</tr>
<tr>
<td>Au</td>
<td>11/7/94</td>
<td>2000-6500 eV</td>
</tr>
<tr>
<td>Li</td>
<td>11/15/94</td>
<td>2000-30000 eV</td>
</tr>
<tr>
<td>Si</td>
<td>6/95</td>
<td>30-500 eV</td>
</tr>
<tr>
<td>Fe</td>
<td>10/95</td>
<td>600-800 eV</td>
</tr>
<tr>
<td>Mo</td>
<td>11/97</td>
<td>10-930 eV</td>
</tr>
<tr>
<td>Be</td>
<td>8/04</td>
<td>40-250 eV</td>
</tr>
<tr>
<td>Mo</td>
<td>8/04</td>
<td>25-60 eV</td>
</tr>
<tr>
<td>W</td>
<td>8/04</td>
<td>35-250 eV</td>
</tr>
<tr>
<td>Ru</td>
<td>8/04</td>
<td>40-1300 eV</td>
</tr>
<tr>
<td>Ti</td>
<td>8/04</td>
<td>20-150 eV</td>
</tr>
<tr>
<td>Sc</td>
<td>4/06</td>
<td>50-1300 eV</td>
</tr>
<tr>
<td>Gd</td>
<td>6/07</td>
<td>12-450 eV</td>
</tr>
<tr>
<td>La</td>
<td>6/07</td>
<td>14-440 eV</td>
</tr>
</tbody>
</table>

Data available at:


class Xray (element)

Bases: object

X-ray scattering properties for the elements. Refer help(periodictable.xsf) from command prompt for details.

\[ f_0 (Q) \]

Isotropic X-ray scattering factors \( f_0 \) for the input \( Q \).

Parameters

\( Q \) [float or vector in [0, 24*pi] | inv A] X-ray scattering properties for the elements.

Returns

\( f_0 \) [float] Values outside the valid range return NaN.

Note: \( f_0 \) is often given as a function of \( \sin(\theta)/\lambda \) whereas we are using \( Q = 4*\pi*\sin(\theta)/\lambda \), or in terms of energy \( Q = 4*\pi*\sin(\theta)*E/(h*c) \).
**scattering_factors** *(energy)*

X-ray scattering factors f', f''.

**Parameters**

- *energy* [float or vector | keV] X-ray energy.

**Returns**

- *scattering_factors* [(float, float)] Values outside the range return NaN.

**Algorithm** Linear interpolation within the Henke Xray scattering factors database at the Lawrence Berkeley Laboratory Center for X-ray Optics.

**sld** *(wavelength=None, energy=None)*

X-ray scattering length density.

**Parameters**

- *wavelength* [float or vector | Å] Wavelength of the X-ray.
- *energy* [float or vector | keV] Energy of the X-ray (if *wavelength* not specified).

**Returns**

- *sld* [(float, float) | inv Å²] (real, imaginary) X-ray scattering length density.

**Raises** *TypeError*: neither *wavelength* nor *energy* was specified.

**Algorithm** The element SLD is r_eN(f1+1jf2), where r_e is the electron radius and N is number density = density/mass * Avogadro’s Number.

The constants are available directly:

- *r_e* = periodic_table.xsf.electron_radius
- *N_A* = periodic_table.constants.avogadro_number

Data comes from the Henke Xray scattering factors database at the Lawrence Berkeley Laboratory Center for X-ray Optics.

**sftable**

X-ray scattering factor table (E,f1,f2)

**init** *(table, reload=False)*

**init_spectral_lines** *(table)*

Sets the K_alpha and K_beta1 wavelengths for select elements

**xray_energy** *(wavelength)*

Convert X-ray wavelength to energy.

**Parameters** *wavelength* : float or vector | Å

**Returns** *energy* : float or vector | keV

**xray_wavelength** *(energy)*

Convert X-ray energy to wavelength.

**Parameters** *energy* : float or vector | keV

**Returns**

**Algorithm** Use the formula:
\[ \lambda = \frac{h}{c} \]

where:
\[ h = \text{planck's constant in eV s} \quad c = \text{speed of light in m/s} \]

```
xray_sld(compound, density=None, wavelength=None, energy=None)
```
Compute xray scattering length densities for molecules.

**Parameters**
- `compound`: [Formula initializer] Chemical formula initializer.
- `density`: [float | g/cm^3] Density of the compound.
- `energy`: [float | keV] Energy of the X-ray, if `wavelength` is not specified.

**Returns**
- `sld`: [(float, float) | 10^-6 inv A^2] (real, imaginary) scattering length density.

**Raises** `AssertionError`: `density` or `wavelength/energy` is missing.

```
xray_sld_from_atoms(*args, **kw)
```
Deprecated since version 0.91: `xray_sld()` now accepts dictionaries of `atom: count` directly.

```
emission_table(table=None)
```
Prints a table of emission lines.

**Parameters**
- `table`: [PeriodicTable.] The default periodictable unless a specific table has been requested.

**Returns** None

```
sld_table(wavelength, table=None)
```
Prints the xray SLD table for the given wavelength.

**Parameters**
- `wavelength`: [float | A] X-ray wavelength.
- `table`: [PeriodicTable] The default periodictable unless a specific table has been requested.

**Returns** None

```
plot_xsf(el)
```
Plots the xray scattering factors for the given element.

**Parameters**
- `el`: Element

**Returns** None

## 2.9 Magnetic Form Factor

### 2.9.1 `periodictable.magnetic_ff`

Adds magnetic_ff[charge].t for t in j0, j2, j4, j6, and J. J should be the dipole approximation \(<j0> + (1 - 2/g) <j2>\), according to the documentation for CrystFML\(^{15}\), but that does not seem to be the case in practice.

\(^{15}\) Brown, P. J. (Section 4.4.5) International Tables for Crystallography Volume C, Wilson, A. J. C.(ed).
class MagneticFormFactor():
    Bases: object

    Magnetic form factor for the ion.

    The available form factors are:

    M = \langle j_0 \rangle form factor coefficients
    J = \langle j_0 \rangle + C_2 \langle j_2 \rangle form factor coefficients
    jn = \langle j_n \rangle form factor coefficients for n = 0, 2, 4, 6

    Not all form factors are available for all ions. Use the expression `hasattr(ion.magnetic_ff, '\'<ff>'\')` to test for the particular form factor `<ff>`. The form factor coefficients are a tuple (A, a, B, b, C, c, D). The following expression computes the M/j0 and J form factors from the corresponding coefficients:

    \[
    s = q^2 / 16 \pi^2 \\
    ff = A \exp(-a \ s^2) + B \exp(-b \ s^2) + C \exp(-c \ s^2) + D
    \]

    The remaining form factors \( j_2 \), \( j_4 \) and \( j_6 \) are scaled by an additional \( s^2 \). The form factor calculation is performed by the `<ff>_Q` method for `<ff>` in \( M, j_0, j_2, j_4, j_6 \). For example, here is the calculation for the \( M \) form factor for Fe\(^{2+}\) computed at 0, 0.1 and 0.2:

    >>> import periodictable
    >>> ion = periodictable.Fe.ion[2]
    >>> print ion.magnetic_ff[ion.charge].M_Q([0, 0.1, 0.2])
    [ 1.099935255  0.99741366]

    \( J_Q(Q) \)
    Returns \( J \) scattering potential at \( Q \) (inverse Angstroms)

    \( M_Q(Q) \)
    Returns \( j_0 \) scattering potential at \( Q \) (inverse Angstroms)

    \( j_0_Q(Q) \)
    Returns \( j_0 \) scattering potential at \( Q \) (inverse Angstroms)

    \( j_2_Q(Q) \)
    Returns \( j_2 \) scattering potential at \( Q \) (inverse Angstroms)

    \( j_4_Q(Q) \)
    Returns \( j_4 \) scattering potential at \( Q \) (inverse Angstroms)

    \( j_6_Q(Q) \)
    Returns \( j_6 \) scattering potential at \( Q \) (inverse Angstroms)

    \( M \)
    \( j_0 \)

    formfactor_0 (\( j_0 \), q)
    Returns the scattering potential for form factor \( j_0 \) at the given \( q \).

    formfactor_n (\( j_n \), q)
    Returns the scattering potential for form factor \( j_n \) at the given \( q \).

    init (table, reload=False)
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